

# Power Corrections to Structure Functions

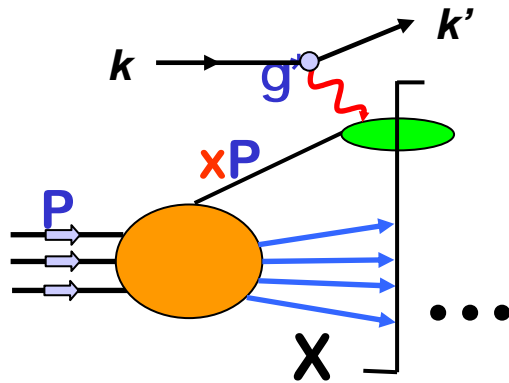
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**DIS 2005 International Workshop, April 27 - May 1, 2005**  
**University of Wisconsin at Madison, Madison, WI**

- ▶ **Structure functions and parton distributions:**
  - Relations to lowest order and leading twist
- ▶ **Electromagnetic current and DIS:**
  - Resumming coherent QCD power corrections
  - Modifications to  $F_2$  and  $F_L$
- ▶ **Weak current and DIS:**
  - Valence and sea quark "shadowing" in  $\nu + A$
  - $F_3$  and QCD sum rules
- ▶ **p+A reactions at RHIC:**
  - Dynamical gluon "shadowing" - particle yields and correlations
- ▶ **Summary:**

# Inclusive Deeply Inelastic Lepton-Hadron Scattering



**Variables:**  $q = k - k'$ ,  $\nu = E - E'$ ,  
 $y = (E - E') / E$ ,  $Q^2 = -q^2$ ,  $x = Q^2 / (2p \cdot q)$

$$\frac{d\sigma_{lh}}{dx dy} = \frac{4\pi\alpha_{em}}{Q^2} \frac{1}{xy} \left[ \frac{y^2}{2} 2xF_1(x, Q^2) + \left( 1 - y - \frac{m_N xy}{2E} \right) F_2(x, Q^2) \right]$$

$F_1(x, Q^2)$ ,  $F_2(x, Q^2)$  - the DIS structure functions

Convenient to **calculate** in a basis of polarization states of  $g^*$

**QCD kicks in with the parton model / factorization**

$$F_T(x, Q^2) = \frac{1}{2} \sum_f Q_f^2 \int d\lambda_0 e^{ix\lambda} \left\langle p \left| \bar{\Psi}(0) \frac{\gamma^+}{2p^+} \Psi(\lambda_0) \right| p \right\rangle$$

$$= \frac{1}{2} \sum_f Q_f^2 \phi_f(x, Q^2) + \mathcal{O}(\alpha_s)$$

$$F_L(x, Q^2) = 0 + \mathcal{O}(\alpha_s)$$

**Lowest Order and Leading Twist relation**

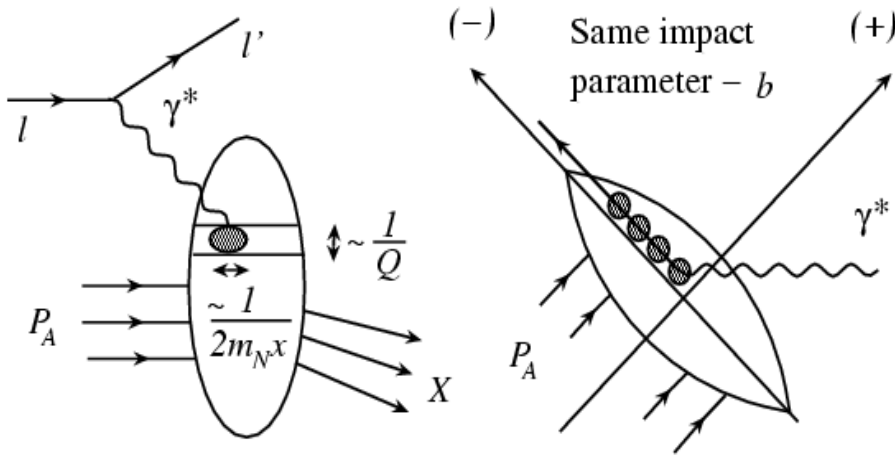
$$F_T(x, Q^2) = F_1(x, Q^2),$$

$$F_L(x, Q^2) = \frac{F_2(x, Q^2)}{2x} - F_1(x, Q^2),$$

$$\text{if } \frac{4x^2 m_N^2}{Q^2} \ll 1$$

Used to determine the parton distribution functions (**PDFs**)

**Both simple and dangerous**



Deviation from A-scaling:  $\sigma_A \neq A \times \sigma$

Longitudinal size:  $\sim 1/2m_N x$

If  $x < 0.1$  then  $\Delta z > r_0$

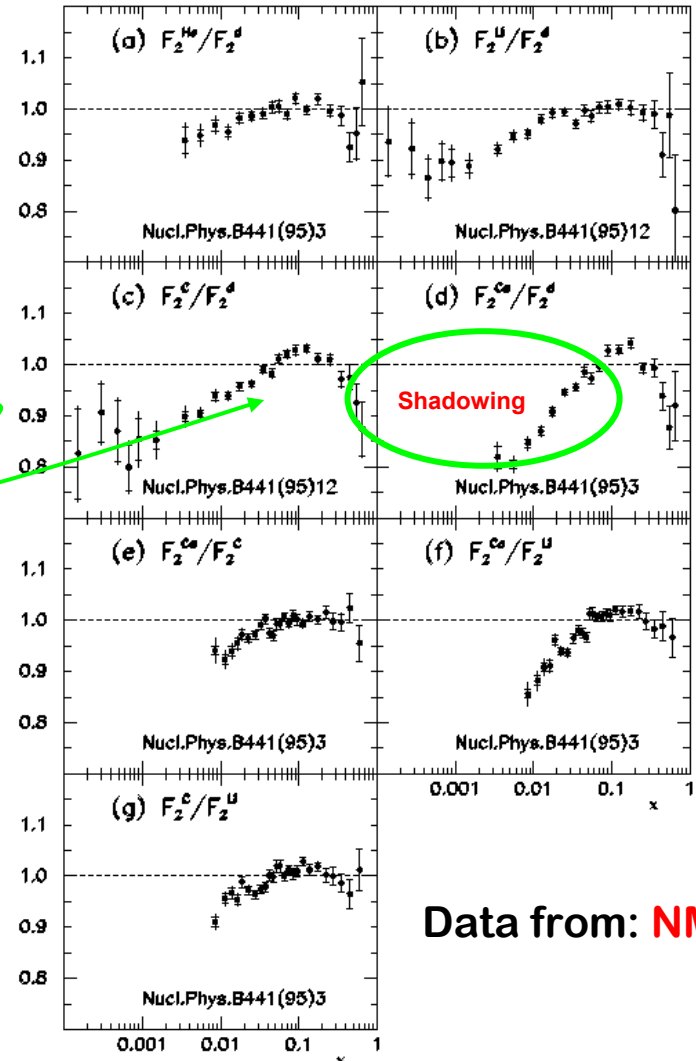
Transverse size:  $\sim 1/Q$

If  $Q < m_N$  then exceed the parton size

What remains for theory:  
power corrections in DIS - suppression

FSI are always present:

S.Brodsky et al., Phys.Rev.D (2002)



Data from: NMC

Ivan Vitev, LANL

# The Idea Behind the Calculation



- Lightcone gauge:  $A \cdot n = A^+ = 0$
  - Breit frame:  $\bar{n} = [1, 0, 0_\perp]$ ,  $n = [0, 1, 0_\perp]$
- $$q = -xp^+ \bar{n} + \frac{Q^2}{2xp^+} n, \quad p = \bar{n} p^+, \quad xp + q = \frac{Q^2}{2xp^+} n$$

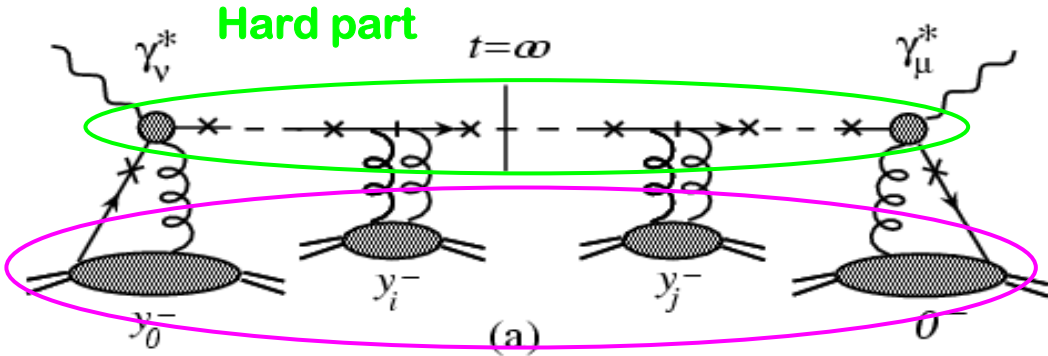
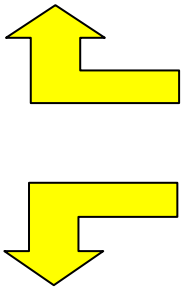
$$Cut = (2\pi) \frac{\gamma^+}{2p^+} \delta(x_i - x_B)$$

$$\Delta(x_i p + q) = \pm i \frac{\gamma^+}{2p^+} \frac{1}{x_i - x \pm i\epsilon} \pm i \frac{xp^+ \gamma^-}{Q^2}$$

↙
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**Long distance**
**Short distance**

*Perturbative*



*Non-perturbative*

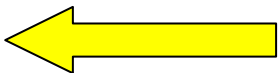
**Matrix element**

$$\langle P | \hat{O}^{T=2+2n} | P \rangle = A \langle P/A | \hat{O}_q^{T=2} | P/A \rangle$$

**Decompose**  $\prod_{i=1}^n \langle P/A | \hat{O}_g^{T=2} | P/A \rangle$

Contribution of single scatter:  $\sim \xi^2 / Q^2$

$$\xi^2 = \left( \frac{3\pi\alpha_s(Q^2)}{8r_{0\perp}^2} \right) \langle p | \hat{F}^2(\lambda_i) | p \rangle$$



$$\hat{F}^2(\lambda_i) = \int \frac{d\tilde{\lambda}_i}{2\pi} \frac{F^{+\alpha}(\lambda_i) F_\alpha^+(\tilde{\lambda}_i)}{(p^+)^2} \theta(\lambda_i - \tilde{\lambda}_i) \Rightarrow \lim_{x \rightarrow 0} \frac{1}{2} x G(x, Q^2)$$

Purely quantum effect

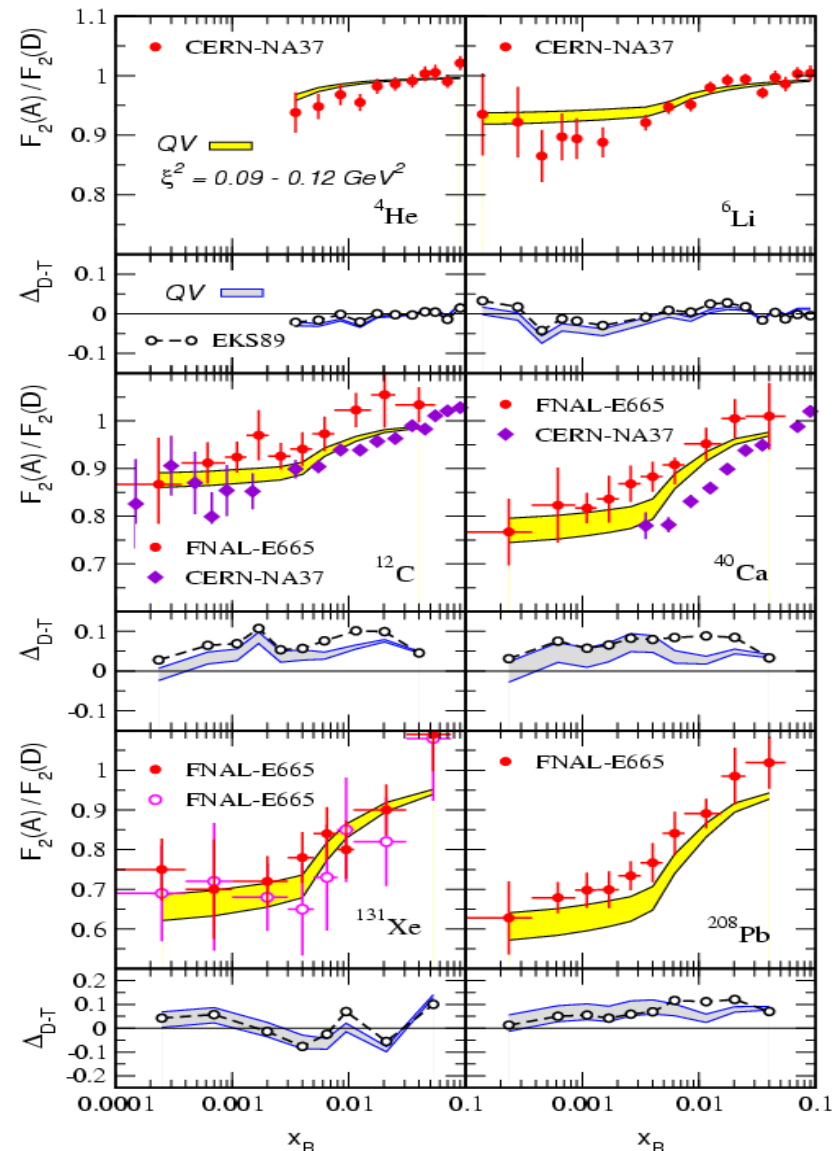
$$\exp \left[ + \frac{\xi^2 (A^{1/3} - 1)}{Q^2} x \frac{d}{dx} \right] F_2(x)$$

$$F_T^A(x, Q^2) \approx A F_T^{(LT)} \left( x + \frac{x \xi^2 (A^{1/3} - 1)}{Q^2}, Q^2 \right)$$

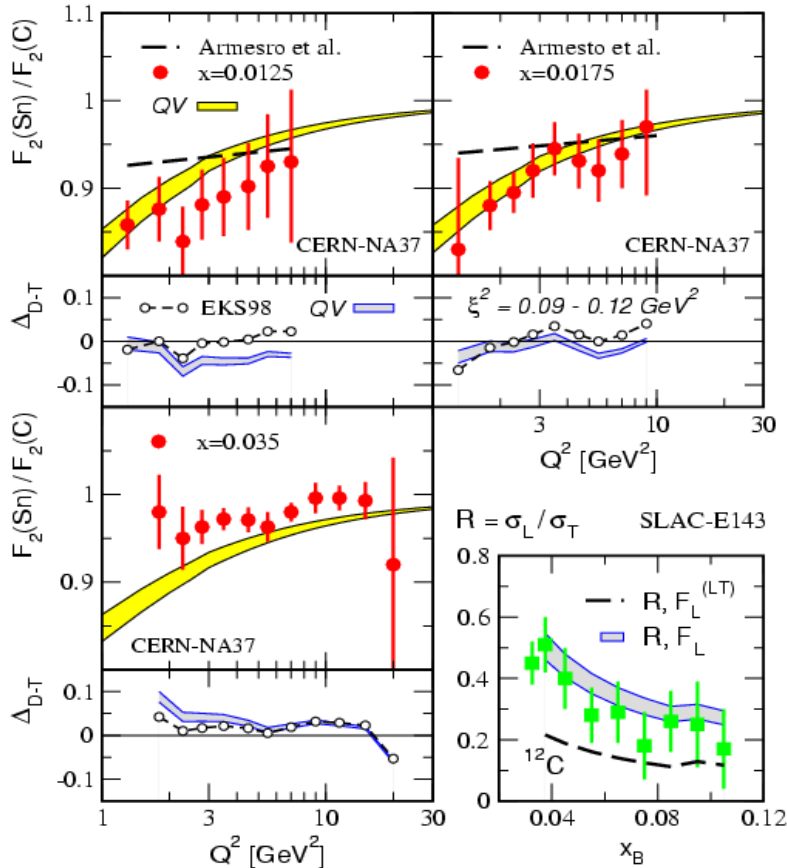
The scale of higher twist per nucleon is small  $\xi^2 \approx 0.1 \text{ GeV}^2$

- Favorable comparison for the  $x$ - and  $A$ -dependence NA37 (NMC) and E665 data
- For  $Q^2 \rightarrow 0$  we impose  $Q^2 = m_N^2$ . (discussion of  $\mathcal{O}(\alpha_s^n)$  and parton size)

J.W.Qiu, I.V., Phys.Rev.Lett. 93 (2004)



# Q<sup>2</sup>-dependence and F<sub>L</sub>(x, Q<sup>2</sup>) from Power Corrections



## Two more tests:

NMC data shows evidence for a power law in  $1/Q^2$  behavior in  $F_2(Sn)/F_2(C)$

$$R(x, Q^2) = \frac{\sigma_L}{\sigma_T} = \frac{F_L(x, Q^2)}{F_1(x, Q^2)}$$

$$F_L^A(x, Q^2) \approx A F_L^{(LT)}(x, Q^2) + \frac{4\xi^2}{Q^2} F_T^A(x, Q^2)$$

J.W.Qiu, I.V., Phys.Rev.Lett.93 (2004)

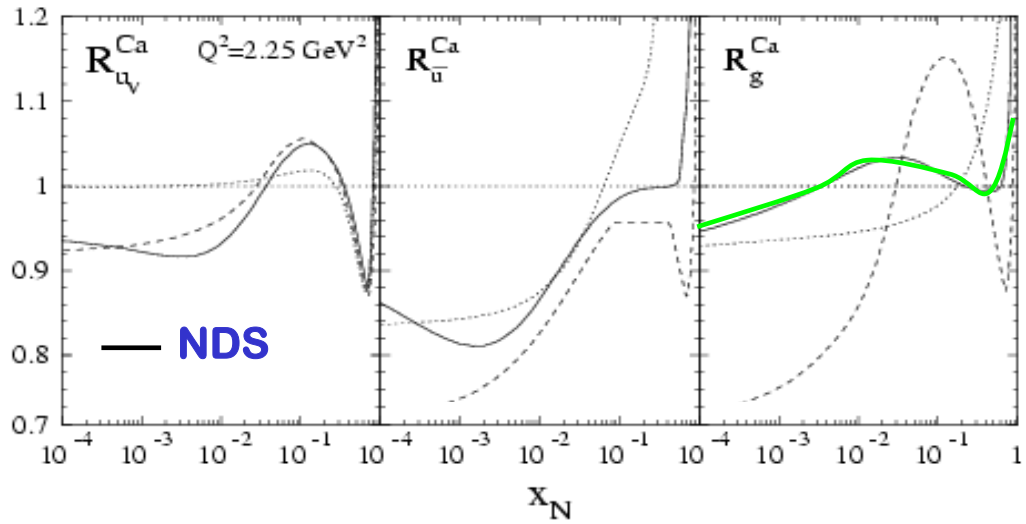
- The Leading Twist (LT)  $R(x, Q^2)$  is not sensitive to modifications of the nPDFs

# How to Check the Origin of Shadowing

## Experimental data

TABLE I: Nuclear data included in the fit.

Measurement	Collaboration	Refs.	# data
$F_2^{He}/F_2^D$	NMC	[13]	18
	SLAC-E139	[14]	18
$F_2^{Be}/F_2^D$	SLAC-E139	[14]	17
$F_2^C/F_2^D$	NMC	[13]	18
	SLAC-E139	[14]	7
$F_2^{Al}/F_2^D$	SLAC-E139	[14]	17
$F_2^{Ca}/F_2^D$	NMC	[13]	18
	SLAC-E139	[14]	7
$F_2^{Fe}/F_2^D$	SLAC-E139	[14]	23
$F_2^{Ag}/F_2^D$	SLAC-E139	[14]	7
$F_2^{Au}/F_2^D$	SLAC-E139	[14]	18
$F_2^{Be}/F_2^C$	NMC	[15]	15
$F_2^{Al}/F_2^C$	NMC	[15]	15
$F_2^{Ca}/F_2^C$	NMC	[15]	15
$F_2^{Fe}/F_2^C$	NMC	[15]	15
$F_2^{Pb}/F_2^C$	NMC	[15]	15
$F_2^{Sn}/F_2^C$	NMC	[16]	145
$\sigma_{DY}^C/\sigma_{DY}^D$	E772	[17]	9
$\sigma_{DY}^{Ca}/\sigma_{DY}^D$	E772	[17]	9
$\sigma_{DY}^{Fe}/\sigma_{DY}^D$	E772	[17]	9
$\sigma_{DY}^W/\sigma_{DY}^D$	E772	[17]	9
Total			420



D. de Florian, R. Sassot, Phys.Rev.D69 (2004)

Very small (negligible) gluon shadowing

- **Only NLO analysis** is directly sensitive to gluon distributions in the nucleus
- So far only one such analysis with **extremely interesting results**

- **Problematic:** for initial state shadowing models  $C_A/C_F = 2.25$
- **Natural:** for final state resummed power corrections



# Modifications to $\nu + A$ Scattering



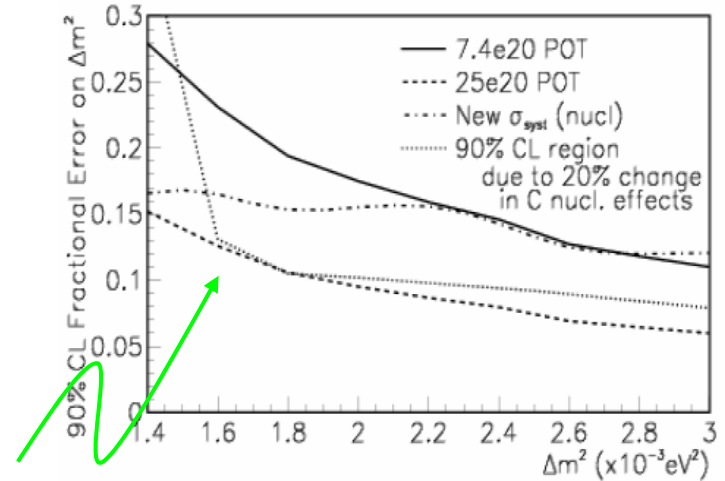
- **No theory** for the shadowing in  $\nu + A$  (exchange  $W^\pm, Z^0$ )
- $3\sigma$  deviation from the Standard Model (Now  $1.8\sigma$ )

$$\sin^2 \theta_W (SM) = 0.2227 \pm 0.0004$$

$$\sin^2 \theta_W (NuTeV) = 0.2277 \pm 0.0013 \pm 0.0009 \pm \dots$$

## NuTeV experiment

G.P.Zeller *et al.*, Phys.Rev.Lett 88 (2002)



- **MINOS** up and running - a case for **MINERvA**

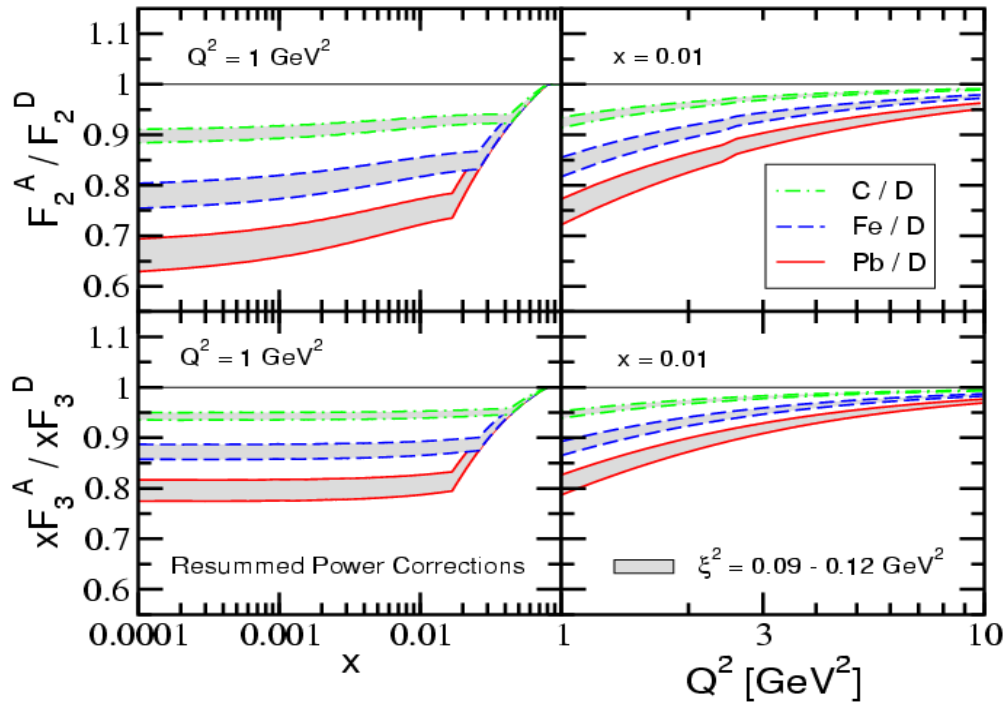
**Cross sections matter**

$$\frac{d\sigma^{\nu, \bar{\nu}}_{cc}}{dx dy} \propto \frac{1}{(\sin^2 \theta_W)^2} \left[ \frac{y^2}{2} 2xF_1^{W^\pm}(x, Q^2) + \left( 1 - y - \frac{m_N xy}{2E} \right) F_2^{W^\pm}(x, Q^2) \pm \left( y - \frac{y^2}{2} \right) xF_3^{W^\pm}(x, Q^2) \right]$$

**Axial** and **vector** part (weak current)

Similarly for the **neutral current**

# Results: $F_2(x, Q^2)$ and $xF_3(x, Q^2)$



J.W.Qiu, I.V., Phys.Lett.B 587 (2004)

First theory of valance quark shadowing  $xF_3(x)$

$$\phi_{sea}(x) \propto 1/x \quad \phi_{val.}(x) \propto 1/\sqrt{x}$$

$$S_{sea} \propto \phi_{sea}(x + \Delta x) / \phi_{sea}(x) \approx 1 - \frac{\Delta x}{x}$$

$$S_{val} \propto \phi_{val}(x + \Delta x) / \phi_{val}(x) \approx 1 - \frac{1}{2} \frac{\Delta x}{x}$$

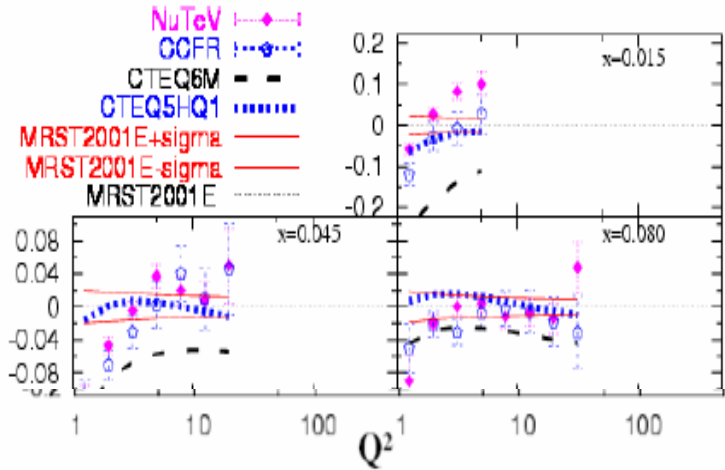
$$x_M = x_B \frac{M^2}{Q^2} \quad x_{\xi^2} = x_B \frac{\xi^2 (A_{1/3} - 1)}{Q^2}$$

$$F_{1,3}^{(\nu W^+)}(x_B, Q^2) = \{2\} A \left( \sum_{D,U} |V_{DU}|^2 \phi_D(x_B + x_{\xi^2} + x_{M_U}) \pm \sum_{\bar{U}, \bar{D}} |V_{\bar{U}\bar{D}}|^2 \phi_{\bar{U}}(x_B + x_{\xi^2} + x_{M_{\bar{U}}}) \right)$$

- Physics:** generation of a dynamical parton mass in the nuclear field

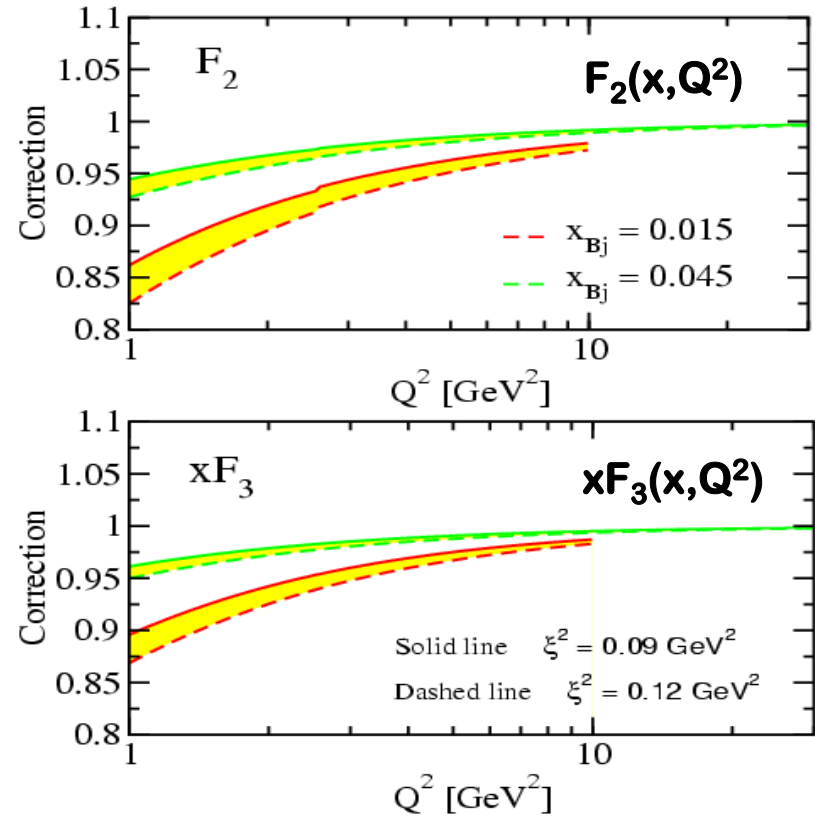
$$x_B \rightarrow x_B \left( 1 + \frac{\xi^2 (A^{1/3} - 1)}{Q^2} + \frac{M^2}{Q^2} \right) = x_B \left( 1 + \frac{m_{dyn}^2 + M^2}{Q^2} \right)$$

## NuTeV / CCFR - DPF 2004 Riverside, CA



Power law deviation between data and the theory

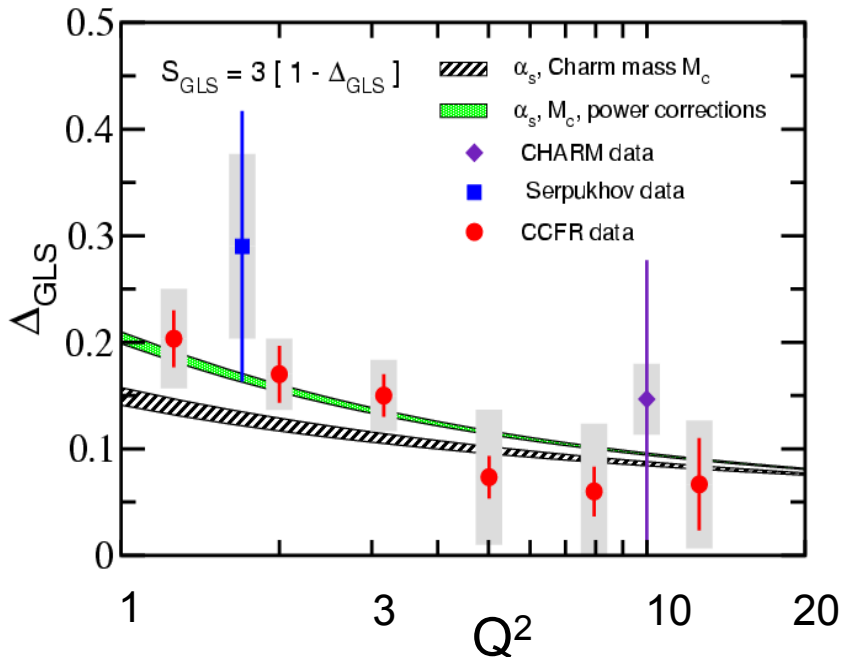
- Focus on the **small  $Q^2$  and  $x < 0.1$  region**
- Look **relative to MRST 2001**. They do not including the nuclear effect in PDFs



J.W.Qiu, I.V., Phys.Lett.B 587 (2004)

Suppression is 12% and 6% in the two lowest x bins at  $Q^2 = 1.3 \text{ GeV}^2$

J.W.Qiu, I.V., Phys.Lett.B 587 (2004)



$$S_{GLS} = \int_0^1 dx \frac{1}{2x} \left( xF_3^{\nu N}(x, Q^2) + xF_3^{\bar{\nu} N}(x, Q^2) \right)$$

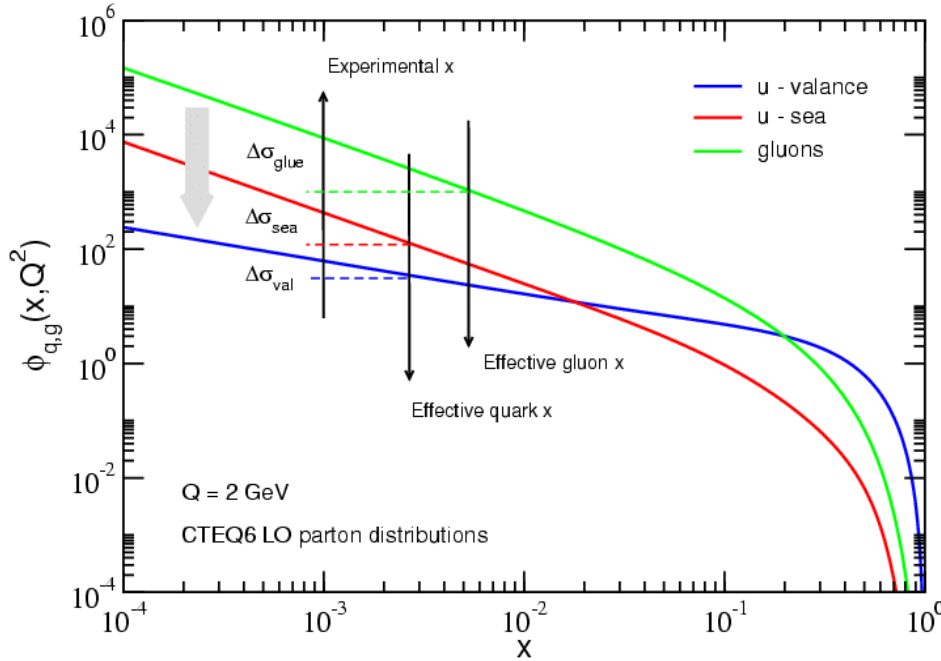
$$= 3(1 - \Delta_{GLS})$$

D.Gross and C.Llewellyn Smith, Nucl.Phys. B 14 (1969)

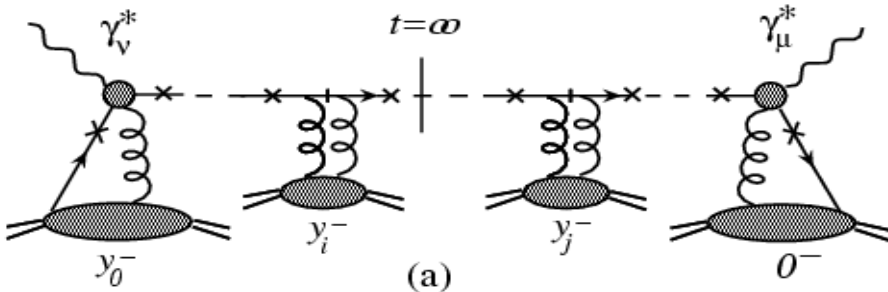
- To Lowest Order (LO)  $S_{GLS} = 3, \Delta_{GLS} = 0$
- At Next-to-Leading Order  $\Delta_{GLS} = \alpha_s / \pi$

- Leading twist shadowing **does not** change the sum rules (only redistributes momentum)
- Neutrino data is **clearly indicative of the high twist nature** of nuclear shadowing

# Summary of the Dynamical Power Corrections



T. Goldman *et al.*, in preparation



- Shadowing in the perturbative regime is calculable based on the **uncertainty principle** and **energy conservation**

- Soft final state interactions generate **dynamical parton mass**  $m^2_{dyn} = \xi^2 A^{1/3}$

- If dictated by the **uncertainty principle**  $x_B < 0.1$  the **energy** of the struck parton should be larger

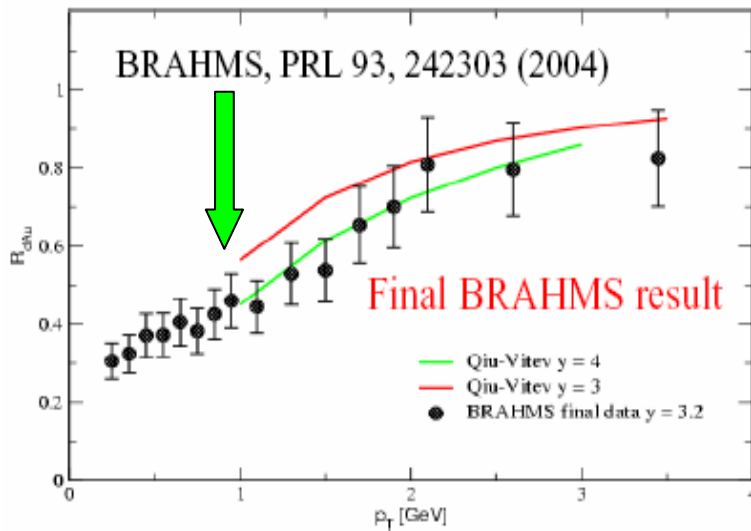
$$x_B \rightarrow x_B \left( 1 + \frac{m^2_{dyn}}{Q^2} \right)$$

- Clearly a **high twist** and **process dependent** effect (final state)

$$S_g > S_{u-sea} > S_{u-val}$$

$$F(x_b) \rightarrow F\left(x_b + x_b C_d \frac{\xi^2}{-t} (A^{1/3} - 1)\right)$$

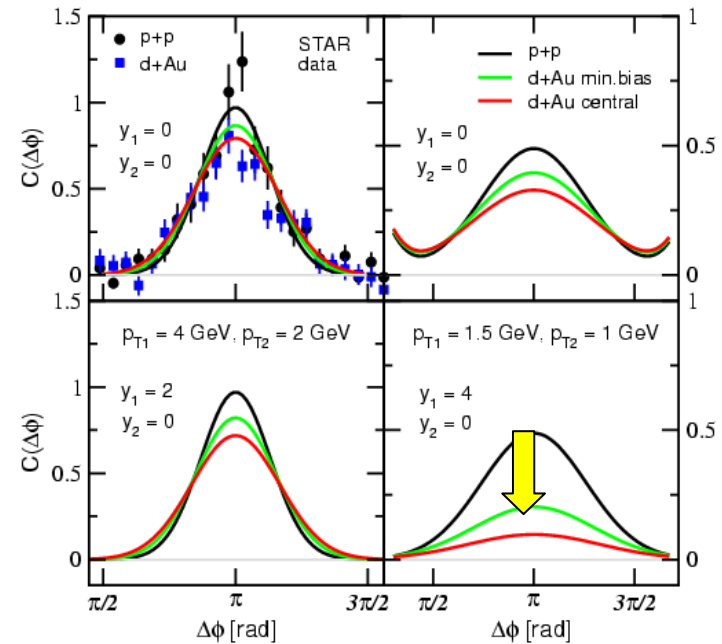
$$F(x_b) = \frac{\phi(x_b)}{x_b} \left| \bar{M}^2_{ab \rightarrow cd} \right|$$



J.W.Qiu, I.V., hep-ph/0405068

Comparison to the data:

I.Arsene *et al.*, Phys.Rev.Lett. 93 (2004)



Suppression **increases** with **rapidity and centrality**

Suppression **disappears** at **high  $p_T$**

Data supports this type of power behavior

# Conclusions

- ▶ **"Shadowing" results from the coherent final state parton scattering with several nucleons (dynamical parton mass, refraction index of nuclear matter for  $q$ ,  $g$ )**
- ▶ **The effect is purely quantum. It enters as a shift of the quantum phase and suppresses the SF exhibits power behavior, i.e. strong  $Q^2$  dependence**
- ▶ **Predicts new high twist contribution to FL. Predicts the difference in sea and valence quark shadowing in neutrino-A reactions and the modification of the QCD sum rules**
- ▶ **For  $p+A$  reactions results can be generalized to dynamical gluon shadowing. Suppression of the hadron yields and correlations**

# New Contribution to $F_L(x, Q^2)$

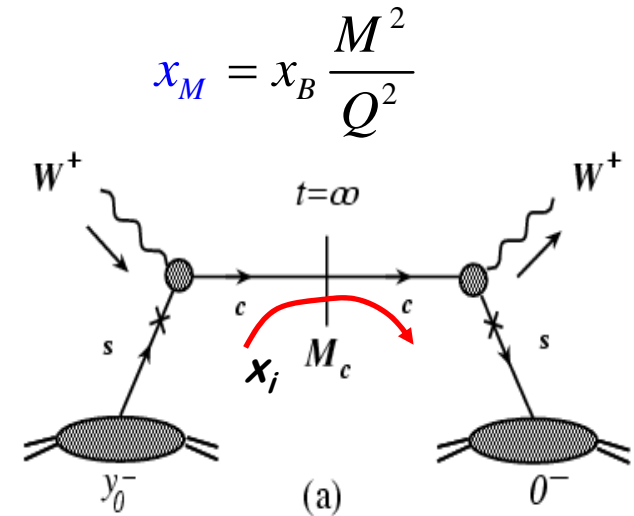


On-shell particle (**M**)

$$Cut = (2\pi) \frac{x_B}{Q^2} (x_M p^+ \gamma^- + (Q^2 / 2x_B p^+) \gamma^+ \pm M) \times \delta(x_i - x_B - x_M) \quad (\text{Cuts fix kinematics})$$

- Even if one neglects  $\phi_c(x, Q^2)$ ,  $\phi_{\bar{c}}(x, Q^2)$  mass effects show up due to the charge exchange

- Along the way we will develop techniques that may be useful in the discussion of charm production at RHIC



J.W.Qiu, I.V., Phys.Lett.B 587 (2004)

$|V|$  - the CKM matrix elements  
 $U = (u, c, t)$ ,  $D = (d, s, b)$

$$F_L^{(\nu W^+)}(x_B, Q^2) = \sum_{D,U} |V_{DU}|^2 \frac{M_U^2}{Q^2} \phi_D(x_B + x_{M_U}) + \sum_{\bar{U}, \bar{D}} |V_{\bar{U}\bar{D}}|^2 \frac{M_{\bar{D}}^2}{Q^2} \phi_{\bar{U}}(x_B + x_{M_{\bar{D}}})$$

$$F_L^{(\bar{\nu} W^-)}(x_B, Q^2) = \sum_{U,D} |V_{UD}|^2 \frac{M_D^2}{Q^2} \phi_U(x_B + x_{M_D}) + \sum_{\bar{D}, \bar{U}} |V_{\bar{D}\bar{U}}|^2 \frac{M_{\bar{U}}^2}{Q^2} \phi_{\bar{D}}(x_B + x_{M_{\bar{U}}})$$



# Mass and Nuclear Enhanced Power Corrections

$$\Delta(xp + q) = \pm i \frac{x_B}{Q^2} p^+ \gamma^- \underbrace{\gamma \cdot \tilde{p}}_{\substack{x_M p^+ \gamma^- + (Q^2 / 2x_B p^+) \gamma^+ \pm M}} \pm i \frac{x_B}{Q^2} \frac{x_M p^+ \gamma^- + (Q^2 / 2x_B p^+) \gamma^+ \pm M}{x - (x_B + x_M) \pm i\epsilon}$$

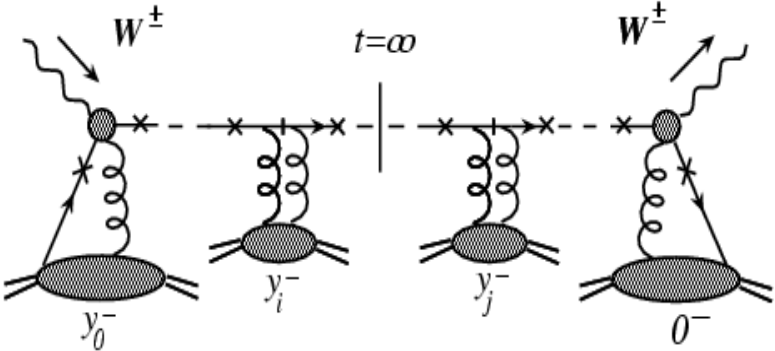
**Special propagator structure:**

$$(\gamma \cdot \tilde{p} + M) \gamma_{\perp} (\gamma \cdot \tilde{p} + M) = 0$$

$$(\gamma \cdot p) \gamma_{\perp} (\gamma \cdot p) = 0$$

- Equations of motion - nuclear enhanced power corrections and mass corrections commute**

- Demonstrated that the corrections can be resummed**



- Physics interpretation – generation of a dynamical parton mass in the nuclear chromomagnetic field**

$$x_B \rightarrow x_B \left( 1 + \frac{\xi^2 (A^{1/3} - 1)}{Q^2} + \frac{M^2}{Q^2} \right) = x_B \left( 1 + \frac{m_{dyn}^2 + M^2}{Q^2} \right)$$